## VANDERBILT UNIVERSITY

## MATH 3120 – INTRO DO PDES HW6

**Question 1.** In class, we proved a theorem about existence of solutions to Poisson's equation in  $\mathbb{R}^n$ . One of the steps of the proof consisted in showing that the function u defined via convolution with the fundamental solution of Laplace's equation is a  $C^2$  function. In class, we showed that u is differentiable. Finish this step of the proof, i.e., show that  $u \in C^2(\mathbb{R}^n)$ .

**Question 2.** Our proof of existence of solutions to Poisson's equation dealt only with  $n \geq 3$ . Establish the theorem in n = 2. For this, follow what we did in class, making the necessary adjustments to the two-dimensional case.